

**Course Syllabus**  
**Mathematics 3FF**  
**2017 – 2018, Semester 2**

Instructor: Walter Craig

Classroom: ABB 271

Course meeting times:

Monday 15:30 - 16:20

Tuesday 16:30 - 17:20

Thursday 15:30 - 16:20

**Lectures:**

**(1) Introduction**

**(2) Wave equations**

- (2.1) transport equations
  - method of characteristics
  - conservation laws
- (2.2) wave equation
  - d'Alembert formula
  - Huygens' principles
- (2.3) method of images
- (2.4) separation of variables
- (2.5) Fourier transform
  - Fourier series
  - Fourier integrals

**(3) The heat equation**

- (3.1) Fourier's law of heat flux
- (3.2) heat kernel
- (3.3) convolution operators
- (3.4) method of images
- (3.5) maximum principle
- (3.6) Hilbert space
- (3.7) heat equation in  $\mathbb{R}^n$
- (3.8) conservation laws and entropy

**(4) Laplace's equation**

- (4.1) boundary value problems
  - Dirichlet problem
  - Neumann problem
  - Poisson problem
- (4.2) Green's identities
- (4.3) fundamental solution
- (4.4) Poisson kernel
- (4.5) maximum principles

**Optional material** (if there is time in our schedule)

**(5) Schrödinger's equation**

- (5.1) quantum mechanics
- (5.2) Heisenberg uncertainty principle
- (5.3) Schrödinger operators

**(6) Hyperbolic conservation laws**

- (6.1) nonlinear conservation laws
- (6.2) Riemann problem
- (6.3) shock waves