

New linear algebra from Terry Tao

- Assume that A is an $n \times n$ Hermitian matrix and M_j is the matrix A with the j^{th} row and column removed.
- Notice that M_j is also Hermitian.
- So suppose that $\lambda_1, \dots, \lambda_n$ are the eigenvalues of A and $\lambda_1^j, \dots, \lambda_{n-1}^j$ are the eigenvalues of M_j for each j .
- Finally, assume that a normalized eigenvector of A for λ_i has the form $(v_1^i, \dots, v_j^i, \dots, v_n^i)$.

Theorem (Denton, Parke, Tao And Zhang)

$$|v_j^i|^2 \prod_{k, k \neq i} (\lambda_i - \lambda_k) = \prod_{k=1}^{n-1} (\lambda_i - \lambda_k^j).$$