

$$\begin{array}{ll}
\text{(BILP(0,0))} & \text{Maximize: } 8y_3 + 3y_4 + 6y_5 + 12y_6 = z \\
& \text{Subject to: } -4y_3 + 2y_4 + 4y_5 + 8y_6 \leq 6 \\
& \quad 4y_3 + 3y_4 + 6y_5 + 12y_6 \leq 15 \\
& \quad 8y_3 + y_4 + 2y_5 + 4y_6 \leq 12 \\
& \quad y_3, \quad y_4, \quad y_5, \quad y_6 \leq 1 \\
& \quad y_3, \quad y_4, \quad y_5, \quad y_6 \geq 0 \\
& \quad y_3, \quad y_4, \quad y_5, \quad y_6 \text{ are integers.}
\end{array}$$

$$y^* = (0, 0, 1, 0, 0, \frac{11}{12}), z = 19$$


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$$\begin{array}{ll}
\text{(BILP(0,1))} & \text{Maximize: } 4 + 8y_3 + 3y_4 + 6y_5 + 12y_6 = z \\
& \text{Subject to: } 4y_3 + 2y_4 + 4y_5 + 8y_6 \leq 8 \\
& \quad 4y_3 + 3y_4 + 6y_5 + 12y_6 \leq 13 \\
& \quad 8y_3 + y_4 + 2y_5 + 4y_6 \leq 8 \\
& \quad y_3, \quad y_4, \quad y_5, \quad y_6 \leq 1 \\
& \quad y_3, \quad y_4, \quad y_5, \quad y_6 \geq 0 \\
& \quad y_3, \quad y_4, \quad y_5, \quad y_6 \text{ are integers.}
\end{array}$$

$$y^* = (0, 1, \frac{11}{20}, 0, 0, \frac{9}{10}), z = \frac{96}{5}$$


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$$\begin{array}{ll}
\text{(BILP(1,0))} & \text{Maximize: } 2 + 8y_3 + 3y_4 + 6y_5 + 12y_6 = z \\
& \text{Subject to: } 4y_3 + 2y_4 + 4y_5 + 8y_6 \leq 7 \\
& \quad 4y_3 + 3y_4 + 6y_5 + 12y_6 \leq 14 \\
& \quad 8y_3 + y_4 + 2y_5 + 4y_6 \leq 10 \\
& \quad y_3, \quad y_4, \quad y_5, \quad y_6 \leq 1 \\
& \quad y_3, \quad y_4, \quad y_5, \quad y_6 \geq 0 \\
& \quad y_3, \quad y_4, \quad y_5, \quad y_6 \text{ are integers.}
\end{array}$$

$$y^* = (1, 0, \frac{4}{5}, 0, 0, \frac{9}{10}), z = \frac{96}{5}$$


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$$\begin{array}{ll}
\text{(BILP(1,1))} & \text{Maximize: } 6 + 8y_3 + 3y_4 + 6y_5 + 12y_6 = z \\
& \text{Subject to: } 4y_3 + 2y_4 + 4y_5 + 8y_6 \leq 9 \\
& \quad 4y_3 + 3y_4 + 6y_5 + 12y_6 \leq 12 \\
& \quad 8y_3 + y_4 + 2y_5 + 4y_6 \leq 6 \\
& \quad y_3, \quad y_4, \quad y_5, \quad y_6 \leq 1 \\
& \quad y_3, \quad y_4, \quad y_5, \quad y_6 \geq 0 \\
& \quad y_3, \quad y_4, \quad y_5, \quad y_6 \text{ are integers.}
\end{array}$$

$$y^* = (1, 1, \frac{3}{10}, 0, 0, \frac{9}{10}), z = \frac{96}{5}$$


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$$\begin{array}{ll}
\text{(BILP(0,0,0))} & \text{Maximize: } 3y_4 + 6y_5 + 12y_6 = z \\
& \text{Subject to: } 2y_4 + 4y_5 + 8y_6 \leq 6 \\
& \quad 3y_4 + 6y_5 + 12y_6 \leq 15 \\
& \quad y_4 + 2y_5 + 4y_6 \leq 12 \\
& \quad y_4, \quad y_5, \quad y_6 \leq 1 \\
& \quad y_4, \quad y_5, \quad y_6 \geq 0 \\
& \quad y_4, \quad y_5, \quad y_6 \text{ are integers.}
\end{array}$$

$$y^* = (0, 0, 0, 0, 0, \frac{3}{4}), z = 9$$


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$$\begin{array}{ll}
\text{(BILP(0,0,1))} & \text{Maximize: } 8 + 3y_4 + 6y_5 + 12y_6 = z \\
& \text{Subject to: } 2y_4 + 4y_5 + 8y_6 \leq 10 \\
& \quad 3y_4 + 6y_5 + 12y_6 \leq 11 \\
& \quad y_4 + 2y_5 + 4y_6 \leq 4 \\
& \quad y_4, \quad y_5, \quad y_6 \leq 1 \\
& \quad y_4, \quad y_5, \quad y_6 \geq 0 \\
& \quad y_4, \quad y_5, \quad y_6 \text{ are integers.}
\end{array}$$

$$y^* = (0, 0, 1, 0, 0, \frac{11}{12}), z = 19$$


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$$\begin{array}{llllll}
\text{(BILP(0,1,0))} & \text{Maximize:} & 4 + 3y_4 & + & 6y_5 & + & 12y_6 & = & z \\
& \text{Subject to:} & 2y_4 & + & 4y_5 & + & 8y_6 & \leq & 8 \\
& & 3y_4 & + & 6y_5 & + & 12y_6 & \leq & 13 \\
& & y_4 & + & 2y_5 & + & 4y_6 & \leq & 8 \\
& & y_4, & & y_5, & & y_6 & \leq & 1 \\
& & y_4, & & y_5, & & y_6 & \geq & 0 \\
& & y_4, & & y_5, & & y_6 & \text{are integers.} & 
\end{array}$$

$y^* = (0, 1, 0, 0, 0, 1)$ ,  $z = 16$  ← **Integer Solution**

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$$\begin{array}{llllll}
\text{(BILP(0,1,1))} & \text{Maximize:} & 12 + 3y_4 & + & 6y_5 & + & 12y_6 & = & z \\
& \text{Subject to:} & 2y_4 & + & 4y_5 & + & 8y_6 & \leq & 4 \\
& & 3y_4 & + & 6y_5 & + & 12y_6 & \leq & 9 \\
& & y_4 & + & 2y_5 & + & 4y_6 & \leq & 0 \\
& & y_4, & & y_5, & & y_6 & \leq & 1 \\
& & y_4, & & y_5, & & y_6 & \geq & 0 \\
& & y_4, & & y_5, & & y_6 & \text{are integers.} & 
\end{array}$$

$y^* = (0, 1, 1, 0, 0, 0)$ ,  $z = 12$  ← **Integer Solution**

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$$\begin{array}{llllll}
\text{(BILP(1,0,0))} & \text{Maximize:} & 2 + 3y_4 & + & 6y_5 & + & 12y_6 & = & z \\
& \text{Subject to:} & 2y_4 & + & 4y_5 & + & 8y_6 & \leq & 7 \\
& & 3y_4 & + & 6y_5 & + & 12y_6 & \leq & 14 \\
& & y_4 & + & 2y_5 & + & 4y_6 & \leq & 10 \\
& & y_4, & & y_5, & & y_6 & \leq & 1 \\
& & y_4, & & y_5, & & y_6 & \geq & 0 \\
& & y_4, & & y_5, & & y_6 & \text{are integers.} & 
\end{array}$$

$y^* = (1, 0, 0, 0, 0, \frac{7}{8})$ ,  $z = \frac{25}{2}$

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$$\begin{array}{llllll}
\text{(BILP(1,0,1))} & \text{Maximize:} & 10 + 3y_4 & + & 6y_5 & + & 12y_6 & = & z \\
& \text{Subject to:} & 2y_4 & + & 4y_5 & + & 8y_6 & \leq & 3 \\
& & 3y_4 & + & 6y_5 & + & 12y_6 & \leq & 10 \\
& & y_4 & + & 2y_5 & + & 4y_6 & \leq & 2 \\
& & y_4, & & y_5, & & y_6 & \leq & 1 \\
& & y_4, & & y_5, & & y_6 & \geq & 0 \\
& & y_4, & & y_5, & & y_6 & \text{are integers.} & 
\end{array}$$

$y^* = (1, 0, 1, 0, 0, \frac{3}{8})$ ,  $z = \frac{29}{2}$

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$$\begin{array}{llllll}
\text{(BILP(1,1,0))} & \text{Maximize:} & 6 + 3y_4 & + & 6y_5 & + & 12y_6 & = & z \\
& \text{Subject to:} & 2y_4 & + & 4y_5 & + & 8y_6 & \leq & 9 \\
& & 3y_4 & + & 6y_5 & + & 12y_6 & \leq & 12 \\
& & y_4 & + & 2y_5 & + & 4y_6 & \leq & 6 \\
& & y_4, & & y_5, & & y_6 & \leq & 1 \\
& & y_4, & & y_5, & & y_6 & \geq & 0 \\
& & y_4, & & y_5, & & y_6 & \text{are integers.} & 
\end{array}$$

$y^* = (1, 1, 0, 0, 0, 1)$ ,  $z = 18$  ← **Integer Solution**

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$$\begin{array}{llllll}
\text{(BILP(1,1,1))} & \text{Maximize:} & 14 + 3y_4 & + & 6y_5 & + & 12y_6 & = & z \\
& \text{Subject to:} & 2y_4 & + & 4y_5 & + & 8y_6 & \leq & 5 \\
& & 3y_4 & + & 6y_5 & + & 12y_6 & \leq & 8 \\
& & y_4 & + & 2y_5 & + & 4y_6 & \leq & -2 \\
& & y_4, & & y_5, & & y_6 & \leq & 1 \\
& & y_4, & & y_5, & & y_6 & \geq & 0 \\
& & y_4, & & y_5, & & y_6 & \text{are integers.} & 
\end{array}$$

Infeasible