

ASSIGNMENT 41

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1. (C) II ... $f(0)$ is not defined

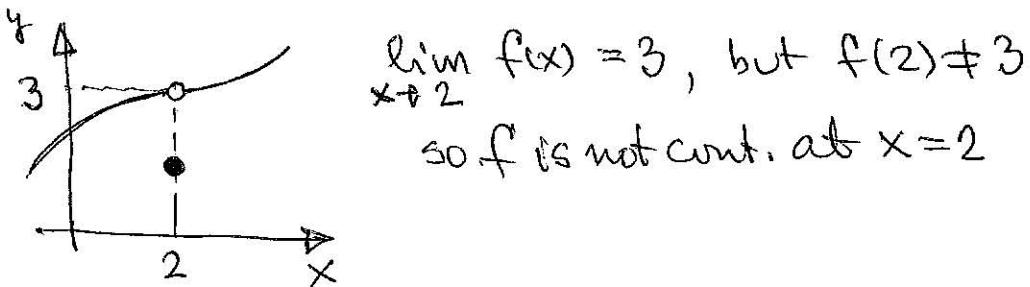
I and III are compositions of continuous functions, and $e^x+1 > 0$, $e^x > 0$ (so that \ln is defined)

2. $f'(x) = \cos(\cos(\sin(\cos x))) \cdot (-\sin(\sin(\cos x)))$.

$$(\text{H}) \quad \cos(\cos(x)) \cdot \underline{(-\sin x)}$$

so $f'(0) = 0$ since x is zero (no need to calculate remaining terms)

3. FALSE; need a counterexample

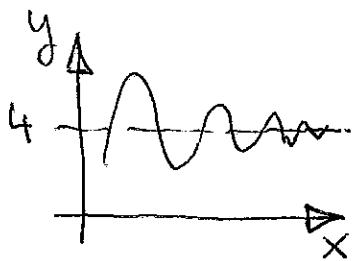


or, algebraic example:

$$f(x) = \begin{cases} x+1 & x \neq 2 \\ 0 & x = 2 \end{cases}$$

4. FALSE; can use same counterexamples as for #3

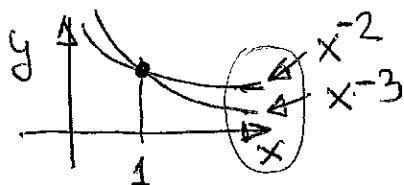
5. FALSE; a function can intersect its horizontal asymptote



f can cross $y = 4$ many times!

6. TRUE ; f is a composition of two continuous functions (\sqrt{x} is cont. when $x \geq 0$)

7. TRUE

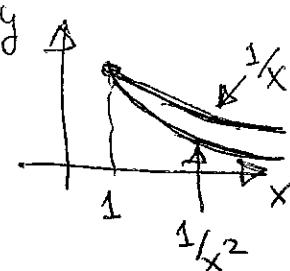


8. FALSE ; need a counterexample

$$\text{let } f(x) = \frac{1}{x}, g(x) = \frac{1}{x^2}$$

$$\text{then } f(x) > g(x) \text{ for } x > 1$$

$$\text{but } \lim_{x \rightarrow \infty} f(x) = \lim_{x \rightarrow \infty} g(x) = 0$$



9. FALSE ; units of $n'(t)$ are monkeys _{day}

→ Units of $\frac{n'(t)}{n(t)}$ are monkeys _{day} / monkey

$$= \frac{1}{\text{day}}$$

10. TRUE ; slope of $y = \cos x$ is

$$y' = -\sin x \dots \text{largest value is 1}$$