

ASSIGNMENT 42

1. $f''(a) > 0 \rightarrow f$ is CU near $a \rightarrow$ I not true
 $f''(a) \neq 0 \rightarrow a$ is not an infl. point \rightarrow II false
 (D) $f'(a) = 0 \rightarrow a$ is a c.p.; since $f''(a) > 0$
 f is CU, so a is a local min.
2. I true, by def. of a critical point
 II true, since $f'(a) =$ slope at a
 (E) III not true (consider $a=0$ for $f(x)=x^3$)
3. FALSE; consider $f(x) = (x-5)^3$, i.e., the graph of x^3 moved 5 units to the right; then $f'(5) = 0$, but $x=5$ is not a local extreme
4. TRUE; Fermat's theorem
5. FALSE; $f(x)$ is continuous for all real numbers, and thus on $[-2, 7]$. By the Extreme Value Theorem, $f(x)$ must have absolute max, and absolute min, in $[-2, 7]$
6. TRUE (exp. function is stronger than any power of x at ∞ ; as well, $x^3 \rightarrow \infty$ as $x \rightarrow \infty$ so the leading behaviour in the denominator is x^3)

7. $m^* = -2$ is an equilibrium (check it)

FALSE $f(x) = 2x^2 + 6x + 2 \rightarrow f'(x) = 4x + 6$

$$f'(m^*) = 4(-2) + 6 = -2 \rightarrow |f'(m^*)| > 1$$

So unstable

8. $f'(x)$ is a polynomial of degree 3, so
FALSE can have at most 3 roots (ie at most
3 critical points)