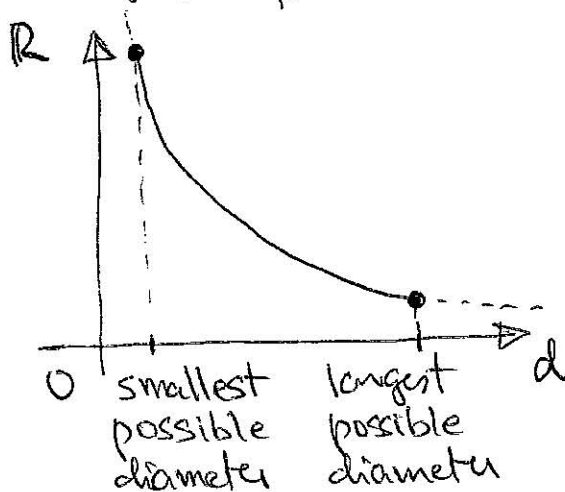


ASSIGNMENT 50

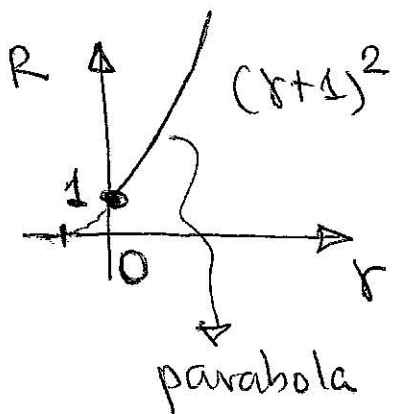
1. (a) R is proportional to viscosity, K
 proportional to the length l of the vessel
 inversely proportional to the fourth power of
 the diameter d

(b) R is of the form $R = \frac{\text{constant}}{d^4}$ (so looks like $y = 1/x^4$)

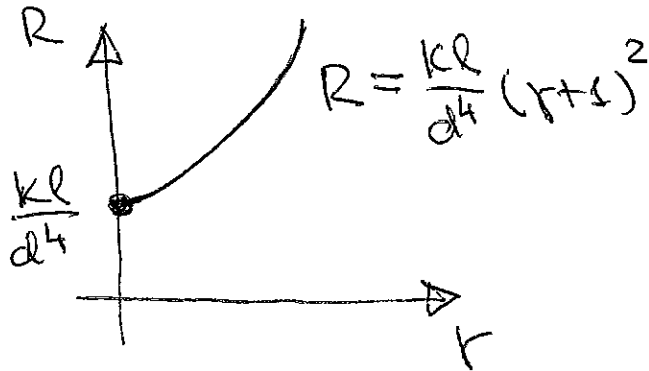


(c) Yes, as the diameter increases, the resistance of the flow decreases. Or: as a blood vessel shrinks the resistance increases.

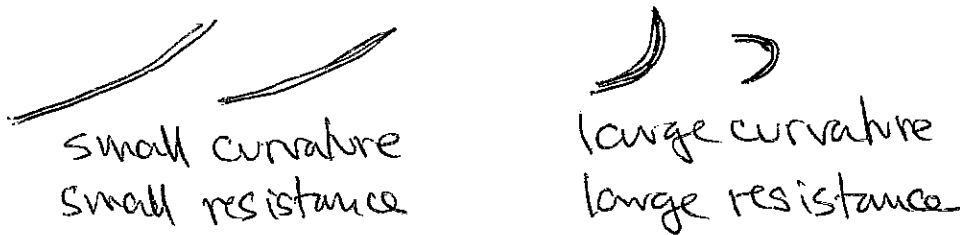
(d) R is of the form $R = \underbrace{\text{constant}}_{\frac{Kl}{d^4}} \cdot (r+1)^2$



If $\frac{Kl}{d^4} < 1 \dots$ compress }
 $\frac{Kl}{d^4} > 1 \dots$ expand } vertically

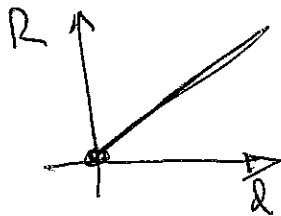


(e) Yes, As the vessel is curved more and more, the resistance increases



(f)
$$R = \frac{kl(r+1)^2}{d^4} = \frac{k(r+1)^2}{d^4} \cdot l$$

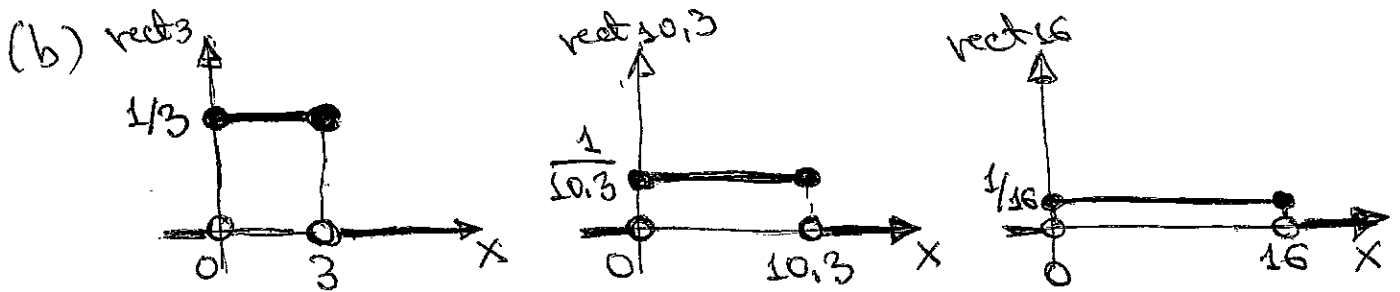
line of slope $k(r+1)^2/d^4$ through the origin in lR -coordinate system



(g)
$$R = \frac{kl(r+1)^2}{d^4} = \frac{l(r+1)^2}{d^4} \cdot k$$

line of slope $\frac{l(r+1)^2}{d^4}$ through the origin in kR -coordinate system.

2. (a) rect_l is a piecewise defined function; between 0 and l (including 0 and l) it is a straight line of height $1/l$; otherwise, i.e., when $x < 0$ and $x > l$ it lies on the x -axis



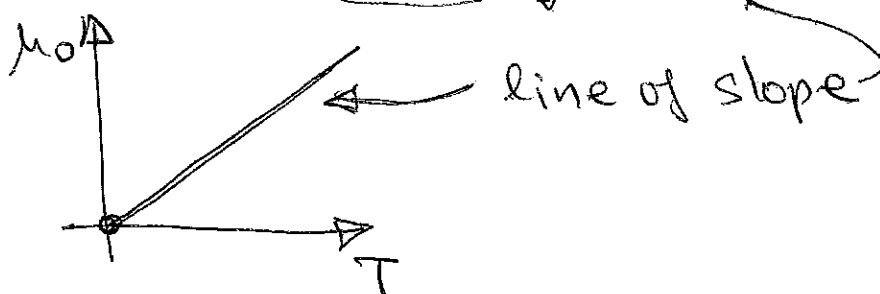
(c) The non-zero horizontal piece of rect_l becomes longer and longer, but comes closer and closer to the x -axis.

3. (a)
$$\mu_0 = \frac{\sqrt{3} k_B T}{4 p l m x_0} \left(\frac{x_0}{2(1-x_0)^3} - \frac{1}{4(1-x_0)^2} + \frac{1}{4} \right) + \frac{\sqrt{3} k_p (n+1)}{4 l_0^{m+1}}$$

line! ↓ slope vertical intercept

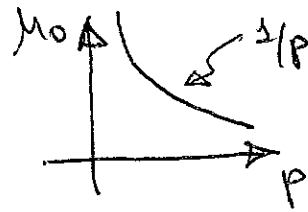
(b)
$$\mu_0 = \frac{\sqrt{3} k_B T}{4 p l m \cdot \frac{1}{2}} \left(\frac{\frac{1}{2}}{\frac{1}{4}} - \frac{1}{1} + \frac{1}{4} \right) + 0$$

$$\mu_0 = \frac{\sqrt{3} k_B \cdot 5}{8 p l m} T$$

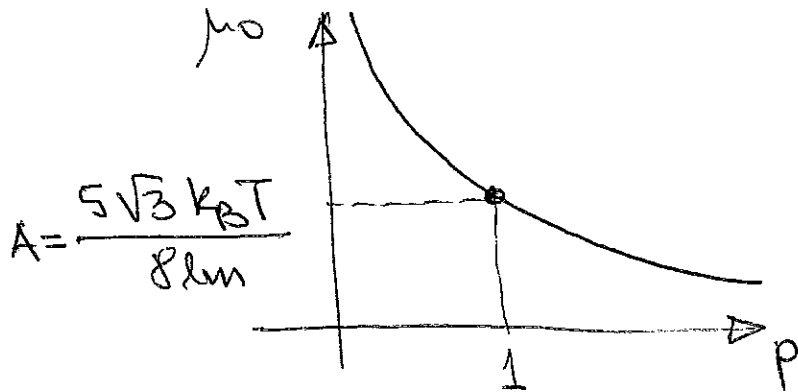


(c) Rewrite μ_0 from (b) as

$$\mu_0 = \frac{5\sqrt{3}k_B T}{8 \ell m} \cdot \frac{1}{P}$$

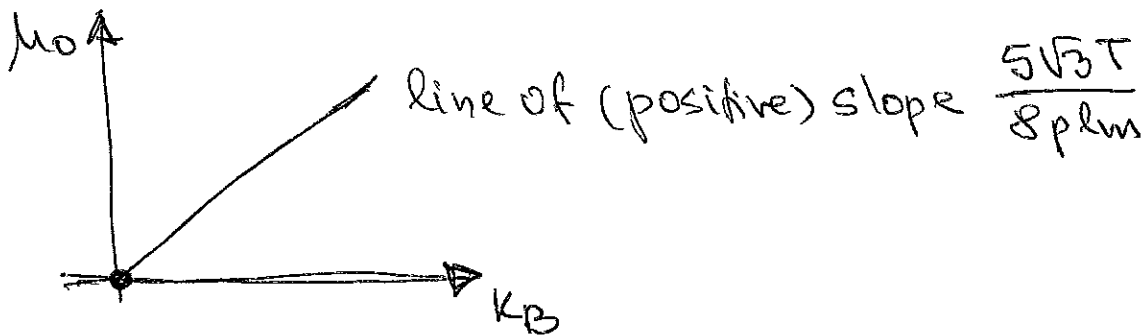


this is constant, call it A

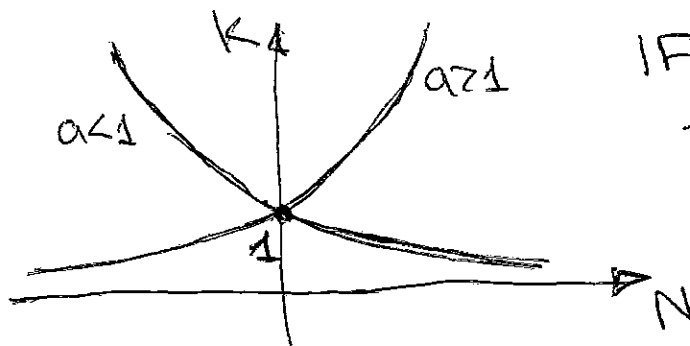


if $A > 1$ expand $\frac{1}{P}$
 if $A < 1$ compress $\frac{1}{P}$
 vertically by a factor of A

(d) Rewrite μ_0 from (b) as $\mu_0 = \frac{5\sqrt{3}T}{8 P \ell m} k_B$



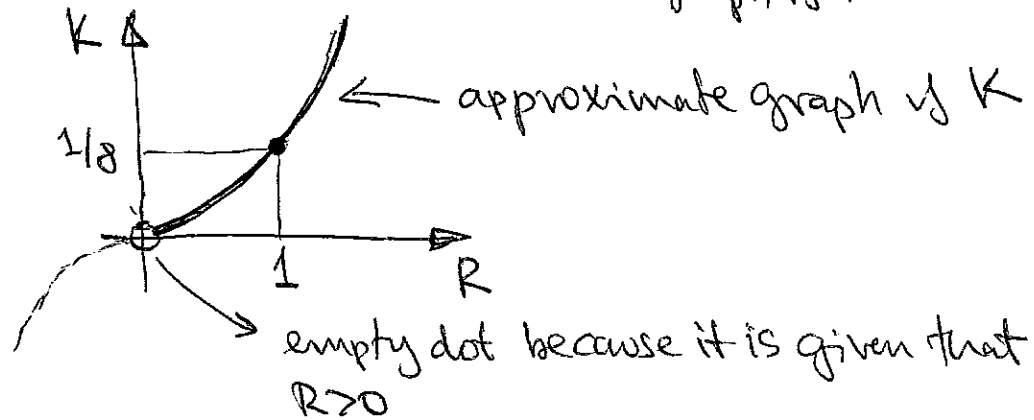
4(a) $K \approx \left(\frac{5R}{\sigma E}\right)^N = a^N$ where $a = \frac{5R}{\sigma E} > 0$



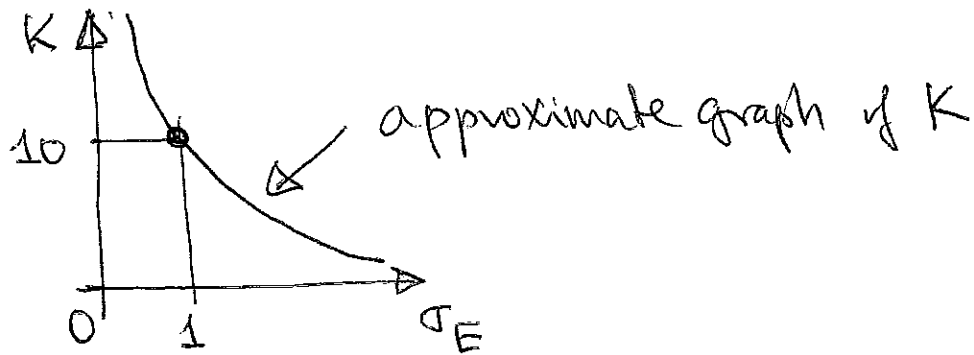
IF $a > 1$ then it is exp. increasing

IF $a < 1$... exp. decreasing
 it could happen that $a = 1$; then the graph of K is
 a horizontal line with intercept 1

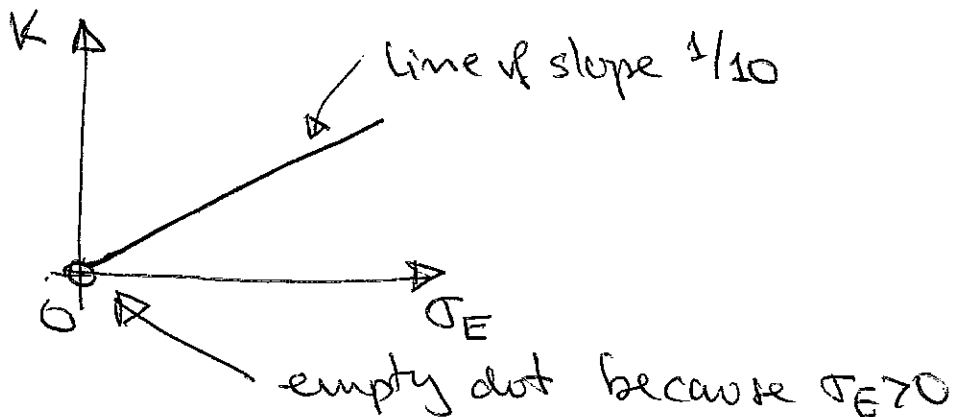
(b) $K \approx \left(\frac{5R}{10}\right)^3 = \left(\frac{R}{2}\right)^3 = \frac{1}{8} R^3$... compressed graph of R^3



(c) $K \approx \left(\frac{5.2}{\sigma_E}\right)^1 = 10 \cdot \frac{1}{\sigma_E}$... vertically expanded graph of $1/\sigma_E$



(d) $K \approx \left(\frac{5.2}{\sigma_E}\right)^{-1} = \frac{1}{10} \sigma_E$



$$(e) \quad K \approx \left(\frac{5R}{\sigma_E} \right)^2$$

$K(R)$

$$\rightarrow K(3R) \approx \left(\frac{5 \cdot 3R}{\sigma_E} \right)^2 = 3^2 \cdot \left(\frac{5R}{\sigma_E} \right)^2 = 3^2 \cdot K(R)$$

increases (approximately) nine-fold

$$(f) \quad K(R) \approx \left(\frac{5R}{\sigma_E} \right)^{-2}$$

$$\rightarrow K(3R) \approx \left(\frac{5 \cdot 3R}{\sigma_E} \right)^{-2} = 3^{-2} \left(\frac{5R}{\sigma_E} \right)^{-2} = \frac{1}{9} \cdot K(R)$$

decreases (approx.) 9-fold

$$(g) \quad K(\sigma_E) \approx \left(\frac{5R}{\sigma_E} \right)^3$$

$$\rightarrow K(2\sigma_E) \approx \left(\frac{5R}{2\sigma_E} \right)^3 = \left(\frac{1}{2} \right)^3 \left(\frac{5R}{\sigma_E} \right)^3 = \frac{1}{8} K(\sigma_E)$$

decreases (approx.) 8-fold

$$(h) \quad K(\sigma_E) \approx \left(\frac{5R}{\sigma_E} \right)^{-1}$$

$$\rightarrow K(2\sigma_E) \approx \left(\frac{5R}{2\sigma_E} \right)^{-1} = \left(\frac{1}{2} \right)^{-1} \left(\frac{5R}{\sigma_E} \right)^{-1} = 2 K(\sigma_E)$$

increases (approx.) 2-fold

i.e. (approx.) doubles