

## Math 2C03 2021 Practice problem set #3 (18430419)

Question

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## Description

stability, nonlinear models, linear first order

## 1. Question Details

ZillDiffEQ9 2.3.004. [3876517]

Find the general solution of the given differential equation.

$$3 \frac{dy}{dx} + 21y = 7$$

 $y(x) =$ Give the largest interval  $I$  over which the general solution is defined. (Think about the implications of any singular points. Enter your answer using interval notation.)

Determine whether there are any transient terms in the general solution.

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## 2. Question Details

ZillDiffEQ9 2.3.005. [3876538]

Find the general solution of the given differential equation.

$$y' + 7x^6y = x^6$$

 $y(x) =$ 

Give the largest interval over which the general solution is defined. (Think about the implications of any singular points. Enter your answer using interval notation.)

Determine whether there are any transient terms in the general solution. (Enter the transient terms as a comma-separated list; if there are none, enter NONE.)

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## 3. Question Details

ZillDiffEq9 2.3.008.MI.SA. [4605519]

*This question has several parts that must be completed sequentially. If you skip a part of the question, you will not receive any points for the skipped part, and you will not be able to come back to the skipped part.*

**Tutorial Exercise**

Find the general solution of the given differential equation.

$$y' = 4y + x^2 + 3$$

Give the largest interval over which the general solution is defined.

Determine whether there are any transient terms in the general solution.

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## 4. Question Details

ZillDiffEq9 2.3.009.EP. [4603923]

Consider the following differential equation.

$$x \frac{dy}{dx} - y = x^2 \sin(x)$$

Find the coefficient function  $P(x)$  when the given differential equation is written in the standard form  $\frac{dy}{dx} + P(x)y = f(x)$ .

$P(x) =$

Find the integrating factor for the differential equation.

$e^{\int P(x) dx} =$

Find the general solution of the given differential equation.

$y(x) =$

Give the largest interval over which the general solution is defined. (Think about the implications of any singular points. Enter your answer using interval notation.)

Determine whether there are any transient terms in the general solution. (Enter the transient terms as a comma-separated list; if there are none, enter NONE.)

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## 5. Question Details

ZillDiffEQ9 2.3.011.EP. [4903660]

Consider the following differential equation.

$$x \frac{dy}{dx} + 2y = x^3 - x$$

Find the coefficient function  $P(x)$  when the given differential equation is written in the standard form  $\frac{dy}{dx} + P(x)y = f(x)$ .

$$P(x) = \text{[input box]}$$

Find the integrating factor for the differential equation.

$$e^{\int P(x) dx} = \text{[input box]}$$

Find the general solution of the given differential equation.

$$y(x) = \text{[input box]}$$

Give the largest interval  $I$  over which the general solution is defined. (Think about the implications of any singular points. Enter your answer using interval notation.)

$$\text{[input box]}$$

Determine whether there are any transient terms in the general solution. (Enter the transient terms as a comma-separated list; if there are none, enter NONE.)

$$\text{[input box]}$$

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## 6. Question Details

ZillDiffEQ9 2.3.012. [3876510]

Find the general solution of the given differential equation.

$$(1 + x) \frac{dy}{dx} - xy = x + x^2$$

$$y(x) = \text{[input box]}$$

Give the largest interval  $I$  over which the general solution is defined. (Think about the implications of any singular points. Enter your answer using interval notation.)

$$\text{[input box]}$$

Determine whether there are any transient terms in the general solution. (Enter the transient terms as a comma-separated list; if there are none, enter NONE.)

$$\text{[input box]}$$

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## 7. Question Details

ZillDiffEQ9 2.3.013. [3876557]

Find the general solution of the given differential equation.

$$x^2 y' + x(x + 2)y = e^x$$

$y(x) =$

Give the largest interval over which the general solution is defined. (Think about the implications of any singular points. Enter your answer using interval notation.)

Determine whether there are any transient terms in the general solution. (Enter the transient terms as a comma-separated list; if there are none, enter NONE.)

**Need Help?**

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## 8. Question Details

ZillDiffEQ9 2.3.015.EP. [4903597]

Consider the following differential equation.

$$y dx - 3(x + y^5) dy = 0$$

Find the coefficient function  $P(y)$  when the given differential equation is written in the standard form  $\frac{dx}{dy} + P(y)x = f(y)$ .

$P(y) =$

Find the integrating factor for the differential equation.

$e^{\int P(y) dy} =$

Find the general solution of the given differential equation.

$x(y) =$

Give the largest interval  $I$  over which the general solution is defined. (Think about the implications of any singular points. Enter your answer using interval notation.)

Determine whether there are any transient terms in the general solution. (Enter the transient terms as a comma-separated list; if there are none, enter NONE.)

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## 9. Question Details

ZillDiffEQ9 2.3.017.EP. [4903600]

Consider the following differential equation.

$$\cos(x) \frac{dy}{dx} + (\sin(x))y = 1$$

Find the coefficient function  $P(x)$  when the given differential equation is written in the standard form  $\frac{dy}{dx} + P(x)y = f(x)$ .

$P(x) =$

Find the integrating factor for the differential equation.

$e^{\int P(x) dx} =$

Find the general solution of the given differential equation.

$y(x) =$

Give the largest interval  $I$  over which the general solution is defined. (Think about the implications of any singular points. Enter your answer using interval notation.)

- ☐  $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$
- ☐  $(0, \pi)$
- ☐  $(-1, 1)$
- ☐  $(-\infty, \infty)$
- ☐  $\left(0, \frac{\pi}{2}\right)$

Determine whether there are any transient terms in the general solution. (Enter the transient terms as a comma-separated list; if there are none, enter NONE.)

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## 10. Question Details

ZillDiffEQ9 2.3.019.EP. [4903601]

Consider the following differential equation.

$$(x + 1)\frac{dy}{dx} + (x + 2)y = 6xe^{-x}$$

Find the coefficient function  $P(x)$  when the given differential equation is written in the standard form  $\frac{dy}{dx} + P(x)y = f(x)$ .

$$P(x) = \text{[input box]}$$

Find the integrating factor for the differential equation.

$$e^{\int P(x) dx} = \text{[input box]}$$

Find the general solution of the given differential equation.

$$y(x) = \text{[input box]}$$

Give the largest interval  $I$  over which the general solution is defined. (Think about the implications of any singular points. Enter your answer using interval notation.)

$$\text{[input box]}$$

Determine whether there are any transient terms in the general solution. (Enter the transient terms as a comma-separated list; if there are none, enter NONE.)

$$\text{[input box]}$$

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## 11. Question Details

ZillDiffEQ9 2.3.023. [3876539]

Find the general solution of the given differential equation.

$$x\frac{dy}{dx} + (5x + 1)y = e^{-5x}$$

$$y(x) = \text{[input box]}$$

Give the largest interval over which the general solution is defined. (Think about the implications of any singular points. Enter your answer using interval notation.)

$$\text{[input box]}$$

Determine whether there are any transient terms in the general solution. (Enter the transient terms as a comma-separated list; if there are none, enter NONE.)

$$\text{[input box]}$$

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## 12. Question Details

ZiilDiffEQ9 2.3.024.EP. [4603913]

Consider the following differential equation.

$$(x^2 - 9) \frac{dy}{dx} + 6y = (x + 3)^2$$

Find the coefficient function  $P(x)$  when the given differential equation is written in the standard form  $\frac{dy}{dx} + P(x)y = f(x)$ .

$$P(x) = \text{[input box]}$$

Find the integrating factor for the differential equation.

$$e^{\int P(x) dx} = \text{[input box]}$$

Find the general solution of the given differential equation.

$$y(x) = \text{[input box]}$$

Give the largest interval over which the general solution is defined. (Think about the implications of any singular points. Enter your answer using interval notation.)

$$\text{[input box]}$$

Determine whether there are any transient terms in the general solution. (Enter the transient terms as a comma-separated list; if there are none, enter NONE.)

$$\text{[input box]}$$

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## 13. Question Details

ZiilDiffEQ9 2.3.025.MI. [4568282]

Solve the given initial-value problem.

$$\frac{dy}{dx} = x + 4y, \quad y(0) = 6$$

$$y(x) = \text{[input box]}$$

Give the largest interval  $I$  over which the solution is defined. (Enter your answer using interval notation.)

$$I = \text{[input box]}$$

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ZillDiffEQ9 2.3.027. [3876555]

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ZillDiffEO9 2.3.031. [4568051]

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ZillDiffEQ9 4.1.001. [3745215]

### Read It

ZillDiffEQ9 4.1.002. [4568033]

### Read It

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## 18. Question Details

ZillDiffEQ9 4.1.004. [4568079]

The given family of functions is the general solution of the differential equation on the indicated interval. Find a member of the family that is a solution of the initial-value problem.

$$y = c_1 + c_2 \cos(x) + c_3 \sin(x), (-\infty, \infty);$$

$$y''' + y' = 0, \quad y(\pi) = 0, \quad y'(\pi) = 3, \quad y''(\pi) = -1$$

$y =$

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## 19. Question Details

ZillDiffEQ9 4.1.009. [3745294]

Find the largest interval which includes  $x = 0$  for which the given initial-value problem has a unique solution. (Enter your answer using interval notation.)

$$(x - 3)y'' + 5y = x, \quad y(0) = 0, \quad y'(0) = 1$$

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## 20. Question Details

ZillDiffEQ9 4.1.017.EP. [4603959]

Consider the following functions.

$$f_1(x) = 6, \quad f_2(x) = \cos^2(x), \quad f_3(x) = \sin^2(x)$$

$$g(x) = c_1 f_1(x) + c_2 f_2(x) + c_3 f_3(x)$$

Solve for  $c_1$ ,  $c_2$ , and  $c_3$  so that  $g(x) = 0$  on the interval  $(-\infty, \infty)$ . If a nontrivial solution exists, state it. (If only the trivial solution exists, enter the trivial solution  $\{0, 0, 0\}$ .)

$\{c_1, c_2, c_3\} = \left\{ \right.$    $\left. \right\}$

Determine whether  $f_1$ ,  $f_2$ ,  $f_3$  are linearly independent on the interval  $(-\infty, \infty)$ .

- ☐ linearly dependent
- ☐ linearly independent

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## 21. Question Details

ZillDiffEQ9 4.1.021.EP. [4603961]

Consider the following functions.

$$f_1(x) = 3 + x, \quad f_2(x) = x, \quad f_3(x) = x^2$$

$$g(x) = c_1 f_1(x) + c_2 f_2(x) + c_3 f_3(x)$$

Solve for  $c_1$ ,  $c_2$ , and  $c_3$  so that  $g(x) = 0$  on the interval  $(-\infty, \infty)$ . If a nontrivial solution exists, state it. (If only the trivial solution exists, enter the trivial solution  $\{0, 0, 0\}$ .)

$$\{c_1, c_2, c_3\} = \left\{ \boxed{\phantom{000}} \right\}$$

Determine whether  $f_1, f_2, f_3$  are linearly independent on the interval  $(-\infty, \infty)$ .

- ☐ linearly dependent
- ☐ linearly independent

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## 22. Question Details

ZillDiffEQ9 4.1.022. [3894055]

Determine whether the given set of functions is linearly independent on the interval  $(-\infty, \infty)$ .

$$f_1(x) = e^x, \quad f_2(x) = e^{-x}, \quad f_3(x) = \sinh(x)$$

- ☐ linearly dependent
- ☐ linearly independent

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## 23. Question Details

ZillDiffEQ9 4.1.022.EP. [4603980]

Consider the following functions.

$$f_1(x) = e^x, \quad f_2(x) = e^{-x}, \quad f_3(x) = \sinh(x)$$

$$g(x) = c_1 f_1(x) + c_2 f_2(x) + c_3 f_3(x)$$

Solve for  $c_1$ ,  $c_2$ , and  $c_3$  so that  $g(x) = 0$  on the interval  $(-\infty, \infty)$ . If a nontrivial solution exists, state it. (If only the trivial solution exists, enter the trivial solution  $\{0, 0, 0\}$ .)

$$\{c_1, c_2, c_3\} = \left\{ \boxed{\phantom{000}} \right\}$$

Determine whether  $f_1, f_2, f_3$  are linearly independent on the interval  $(-\infty, \infty)$ .

- ☐ linearly dependent
- ☐ linearly independent

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## 24. Question Details

ZillDiffEQ9 4.1.023. [3894119]

Consider the differential equation

$$y'' - y' - 6y = 0.$$

Verify that the functions  $e^{-2x}$  and  $e^{3x}$  form a fundamental set of solutions of the differential equation on the interval  $(-\infty, \infty)$ .

The functions satisfy the differential equation and are linearly independent since the Wronskian

$$W(e^{-2x}, e^{3x}) = \boxed{\phantom{000000}} \neq 0 \text{ for } -\infty < x < \infty.$$

Form the general solution.

$$y = \boxed{\phantom{000000}}$$

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## 25. Question Details

ZillDiffEQ9 4.1.025. [4568312]

Consider the differential equation

$$y'' - 2y' + 37y = 0; \quad e^x \cos(6x), e^x \sin(6x), (-\infty, \infty).$$

Verify that the given functions form a fundamental set of solutions of the differential equation on the indicated interval.

The functions satisfy the differential equation and are linearly independent since

$$W(e^x \cos(6x), e^x \sin(6x)) = \boxed{\phantom{000000}} \neq 0 \text{ for } -\infty < x < \infty.$$

Form the general solution.

$$y = \boxed{\phantom{000000}}$$

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## 26. Question Details

ZillDiffEQ9 4.1.027.MI.SA. [4605488]

*This question has several parts that must be completed sequentially. If you skip a part of the question, you will not receive any points for the skipped part, and you will not be able to come back to the skipped part.*

### Tutorial Exercise

Consider the differential equation

$$x^2 y'' - 4xy' + 6y = 0; \quad x^2, x^3, (0, \infty).$$

Verify that the given functions form a fundamental set of solutions of the differential equation on the indicated interval.

Form the general solution.

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## Assignment Details

Name (AID): Math 2C03 2021 Practice problem set #3 (18430419)

Submissions Allowed: 20

Category: Homework

## Feedback Settings

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