

# *Population regulation*

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## *Introduction*

### *The first law of population dynamics*

- If individuals are behaving independently:
- the population-level rate of growth (or decline) is proportional to the population size
- the population grows (or declines) exponentially

### *The second law of population dynamics*

- Exponential growth (or decline) cannot continue forever
- Something is changing the average rate at which populations we observe grow

### *The third law of population dynamics*

- The changes in average rate must depend on the population size
- Populations are, directly or indirectly, affecting their own growth rates
- **Density dependence** (or preferably **density-dependent processes**)

### *Long-term growth rates*

- Populations maintain long-term growth rates very close to  $r = 0$
- This is almost certainly because factors affecting their growth rate change with the size of population.
- What is one density-dependent mechanism that could feed back on the growth rate?

## *Population regulation*

- All the populations we see are *regulated*

- On average, population growth is higher when the population is lower
- Maybe with a time delay
- Lots of populations don't *seem* to be regulated

### *Mechanisms of regulation*

- Dense populations experience more within-species competition
- e.g. for food or space: *per capita* resources proportional to  $1/N$
- Dense populations may damage environments or resources that they need
- Dense populations attract more **natural enemies**
- Dense populations may overflow onto poor habitat

### *Regulation may be hard to see*

- Some species seem to completely fill a niche (mangroves), or deplete their own food resources (rabbits)
- Other species seem like they could easily be more common (pine trees)
- May be controlled by cryptic (hard to see) natural enemies (disease, parasites)
- May be controlled by food limitation at bad times (e.g., droughts)
- Density **vagueness** (Strong 1986) ?
- Ecological data are **noisy**: need statistical methods to see regulation
- In the long term, every species is controlled in part by factors which respond to the species population size
- Otherwise, in the long term, it would increase forever or decline to extinction (random walk)

### *Regulation works over the long term*

- Not every species experiences population regulation all the time
- Maybe expanding into a niche (e.g., because of climate change)
- Maybe controlled by big outbreaks of disease
- Maybe species outbreaks into marginal habitat, and spends most of the time contracting back to their “core” habitat

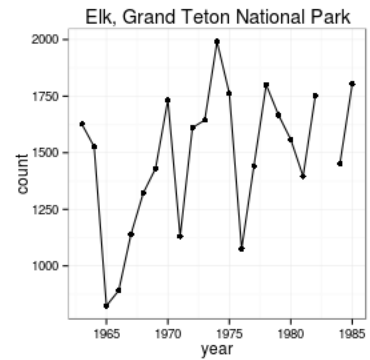


Figure 1: plot of chunk elk1



Figure 2: rabbits in New Zealand

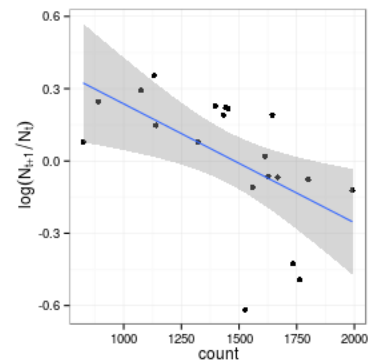


Figure 3: plot of chunk elkdiff

### *How do we know it's regulation?*

- Why don't we believe that population growth is controlled by factors that don't depend on the population itself?

### *The great density-dependence debate*

- Ecologists spent 40 years arguing about how important density-dependent processes are (Schmitt, Holbrook, and Osenberg 1999)
- *Field ecologists*: "We see strong density-independent processes operating!"
- *Theoreticians*: "There must be density-dependence somewhere!"
- Leaky bucket:  $dW/dt = [\text{input}] - [\text{leakiness}]W \rightarrow W^* = [\text{input}]/[\text{leakiness}]$
- Field ecologists are right: *variation* in D-I processes explains lots of the *variation* we see
- Theoreticians are right: D-D most likely  $> 0$  for most species
- Statisticians are right: better methods for measuring D-D (Dennis and Taper 1994)

### *Modeling framework*

#### *Modeling*

- Start with a discrete-time or continuous-time population model
- How can we add regulation?

#### *Density-dependent processes*

- How do *per capita* **vital rates** (birth rate, death rate) change with population density?
- *Shape*: is the response straight, curved, curved more than once?
- *Scale*: how much does additional density affect vital rates?
- Two curves may have the same shape but different scales
- When does the curve cross zero?
- What does the zero-crossing point mean?

*Different scales (per capita)*

*Different scales (absolute growth)*

*Different shapes (per capita)*

*Different shapes (absolute)*

*Mathematical details*

- Linear *per capita* rates: **logistic model**,  $r(N) = r_0(1 - N/K)$
- Do birth rates, or death rates, or both, change?
- Maybe we only care about  $r(N) = b(N) - d(N)$
- If birth, have to stop at  $b(N) = 0$ ; can chop it off but this is unrealistic/mathematically ugly
- Mortality rate can grow arbitrarily large (lifespan approaches zero)

*Mathematical details (2)*

- More flexible model: **theta-logistic model**,  $r(N) = r_0(1 - (N/K)^\theta)$
- Have to be careful when  $\theta < 0$
- Hard to separate birth and death: **phenomenological** model (vs. **mechanistic** alternatives)
- Hard to estimate: (Sæther, Engen, and Matthysen 2002; Sibly et al. 2005; Clark et al. 2010)

*Another model*

- In principle we can pick *any* model with decreasing (or constant) fecundity and increasing (or constant) birth rates
- *exponential-fecundity* model
- constant death rates,  $d(N) \equiv d$
- birth rate declines exponentially with density,  $b(N) \equiv b(0) \exp(-N/N_b)$
- What are the units of  $N_b$ ?

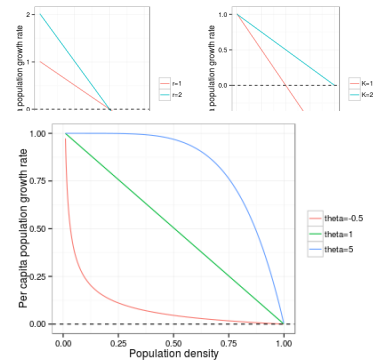


Figure 6: plot of chunk shape1

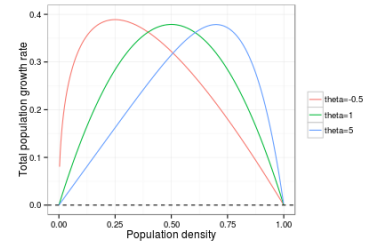


Figure 7: plot of chunk shape2

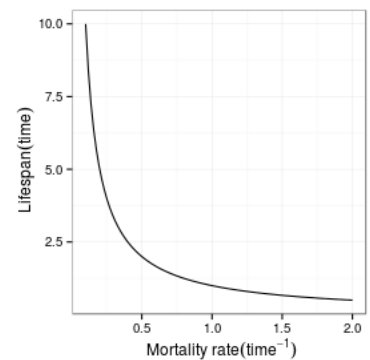


Figure 8: plot of chunk mort1

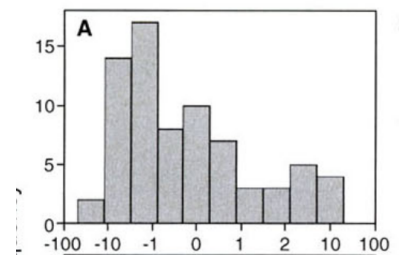


Figure 9:  $\theta$  for mammal populations (Sibly et al. 2005)

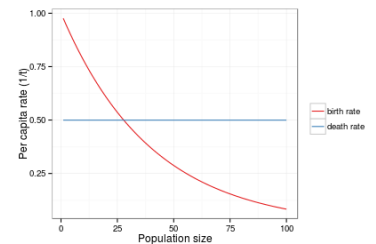
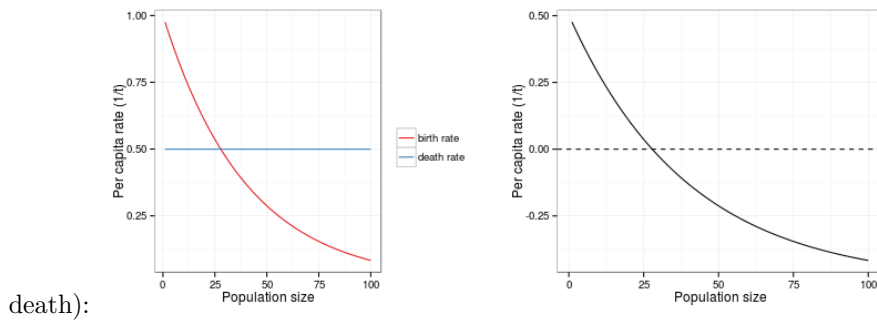


Figure 10: plot of chunk fecmodel

### Another model

- can also reduce the model from birth & death to growth (birth-



death):

### Continuous-time models

#### Mathematical model

- Suppose population has constant *per capita* birth rates  $b(N)$  and death rates  $d(N)$
- Our mathematical model is:  $\frac{dN}{dt} = (b(N) - d(N))N \equiv r(N)N$
- This tells us how fast the population is changing at any instant
- Recall: when we model a population using its size, we are assuming we can treat all individuals as the same

#### Recruitment

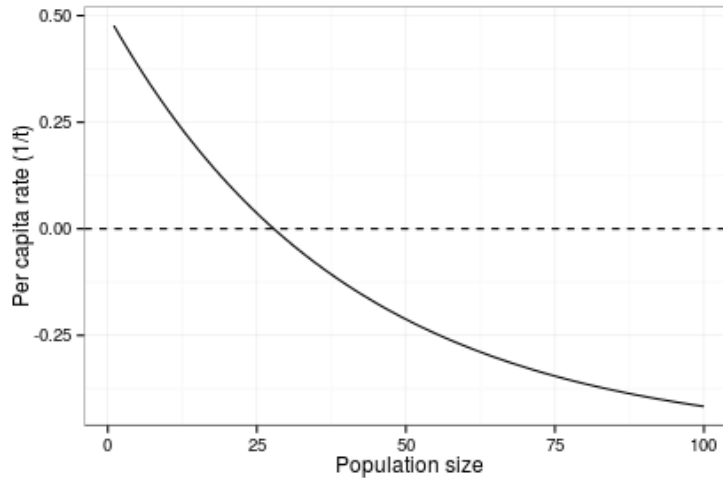
- **Recruitment** is when an organism moves from one life stage to another
- e.g. Seed  $\rightarrow$  seedling  $\rightarrow$  sapling  $\rightarrow$  tree
- Egg  $\rightarrow$  larva  $\rightarrow$  pupa  $\rightarrow$  adult moth
- In simple continuous-time population models, recruitment is included in birth:
- $b$  is the rate at which adults produce new adults (or seeds produce new seeds)

#### Density dependent processes

- What will normally happen to the (per capita) birth rate when population density is high?
- What will normally happen to the (per capita) death rate when population density is high?

### Density-dependent regulation

- “Density dependent” means that:
  - Above some level of population density, the reproductive number  $R$  goes down when density goes up:
  - eventually  $R$  crosses from  $> 1$  to  $< 1$ ,  $r$  from positive to negative



### Model behaviour

#### Dynamics

- What sort of **dynamics** do we expect from our conceptual population?
- i.e., how will it change through time?
- What will the population do if it starts near zero?
- ... near the equilibrium?
- ... at a high value?

#### What will this model do?

Exponential-fecundity model:

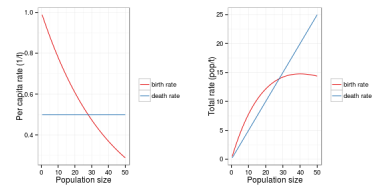


Figure 11: plot of chunk unnamed-chunk-1

### Time dynamics

#### Time dynamics (log scale)

#### Time dynamics (high starting value)

#### Time dynamics (different $\theta$ )

#### Time dynamics (different $\theta$ , log scale)

### Simulations

- We will simulate the behaviour of populations in continuous time using the program R
- <http://lalashan.mcmaster.ca/theobio/3SS/index.php/BirthDeath>

### Characteristic Time

- If a population is growing (or declining) exponentially at rate  $r$ , we can call  $1/r$  the **characteristic time** ( $e$ -folding time) of population change
- Bacteria death example: they are continuously dying at a rate of 0.05 deaths per individuals per hour
- Characteristic time is 20 hours. If the rate *didn't decrease with population size*, they would disappear completely in 20 hours

### Human growth example

- Long-term average growth rate is 0.0003/yr
- When growing at that rate:

### Doubling time

- The characteristic time of growth (decline) is very similar to the doubling time (half life)
- Characteristic time is more closely related to instantaneous dynamics, so it's used more often in dynamic modeling

### Equations

- $N = N_0 \exp(t/T_c)$  for growth
- $N = N_0 \exp(-t/T_c)$  for decline

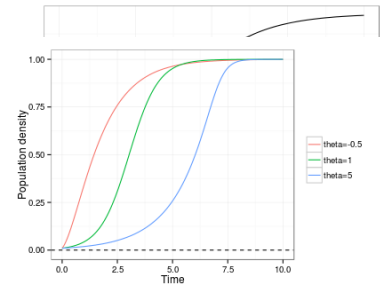


Figure 15: plot of chunk logist\_dt\_theta

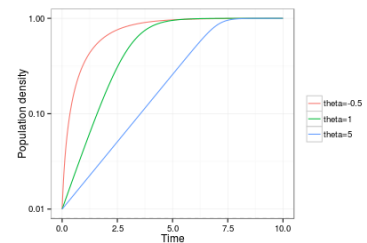


Figure 16: plot of chunk thetalogist\_dt\_log

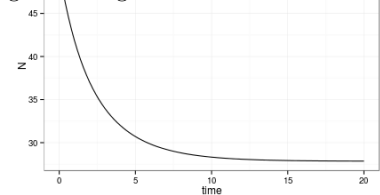


Figure 14: plot of chunk logist\_dt\_high

- If  $t \ll T_c$  change is close to linear
- If  $t \gg T_c$  change (should be) extreme!

### *Characteristic scale*

- A **characteristic scale** for density dependence is analogous to a characteristic time
- We rewrite the exponential equation to have a scale constant with the same units as the population.
- For example:  $b(N) = b_0 \exp(-N/N_b)$
- $N_b$  is the characteristic scale of density-dependence in birth rate
- If  $N \ll N_b$ , density dependence is linear (and weak)
- If  $N \gg N_b$ , density dependence is extreme (virtually no births)

### *Analyzing behaviour*

- Dynamics of density-dependent populations
- Recall  $\frac{dN}{dt} = (b(N) - d(N))N$

### *Equilibria*

- In this simple model, when does equilibrium occur?
- Does our model have any **stable** equilibria?
- Does it have any **unstable** equilibria?

### *Stable and unstable equilibria*

- If we are at an equilibrium we expect to stay there
- At least in our simplified model
- An equilibrium is defined as stable if we expect to approach the equilibrium when we are near it
- An equilibrium is defined as unstable if we expect to move away from the equilibrium when we are near it

### *What kind of equilibrium?*

- How can we tell an equilibrium is stable?
- If population is just below the equilibrium:
- If population is just above the equilibrium:

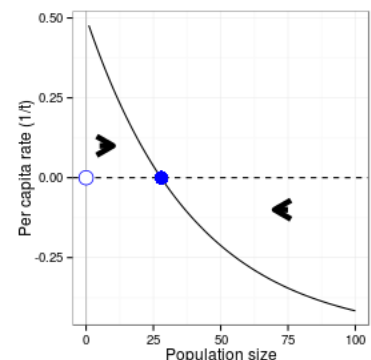


Figure 17: plot of chunk stabplot



*Invasion*

- We say a species can **invade** a community if its rate of change is positive when the population is small.
- In other words, population can invade if the **extinction equilibrium**  $N = 0$  is not stable
- In this conceptual model, this is the same as saying  $b(0) > d(0)$
- We can define a new value  $R_0 = b(0)/d(0)$

*Carrying capacity*

- In a simple system with density dependence:
- When  $R_0 < 1$ ,  $R(N)$  is always  $< 1$ , and the population never persists
- When  $R_0 > 1$ , the population has a single, stable equilibrium:

*Dynamics of density-dependent populations*

- Populations following this model change *smoothly*
- Equations tell how the population will change at each instant
- They have no memory
- Birth rate and death rate are determined by population size alone
- Cycling is impossible

*Dynamics of real-world populations*

- Initial exponential growth and leveling off frequently observed
- Exponential approach to equilibrium hard to observe
- Real populations are subject to **stochastic**(random) effects
- Real populations are subject to changing conditions
- Some species exhibit cycles

*Competition and depletion*

- **Competition** occurs when organisms interfere with each others' use of resources
- Competition may or may not involve **depletion** of resources (reducing the amount of resource available in the future)

### Resource competition

- What is a resource that is competed for but not depleted?

### Conclusion

- We expect models of resource competition *without* depletion to exhibit smooth behaviours:
- The models in this section are not suitable for populations for which resource depletion is important

### Allee effects

#### Small-population effects

- What would happen if I released one butterfly into a new, highly suitable habitat?

#### Allee effects

- Effects which cause small populations to have low per-capita growth rates are called **Allee effects**
- Equivalent to saying that medium-sized populations have larger per-capita growth rates than small ones
- Why might per capita growth rates decrease in small populations?

#### Allee effect models

#### Allee effect example

#### Allee effect: stability analysis

#### Allee effects

- Population may go extinct if it drops below a certain threshold (**strong Allee effect**:  $r(0) < 0$ ,  $R(0) < 1$ )
- **Weak** Allee effect: *per capita* growth rate decreases toward zero, but doesn't go negative ( $r(0) > 0$ ,  $R(0) > 1$ )
- How do populations establish in the presence of Allee effects?

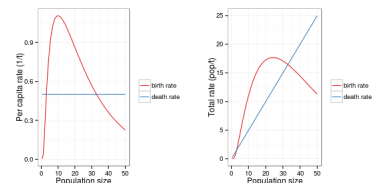


Figure 18: plot of chunky allee1

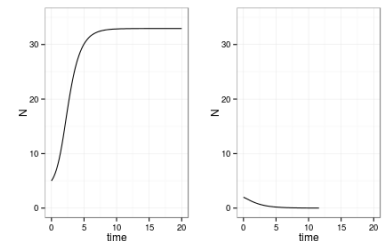


Figure 19: plot of chunky allee2

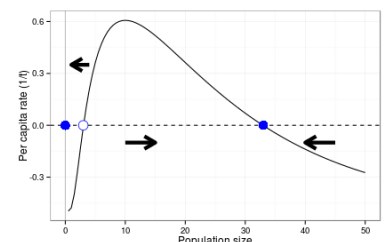


Figure 20: plot of chunky allee3

*Invasion*

- When Allee effects are present, it's no longer true that a species that can't invade can't persist
- We may have  $R_0 < 1$ , but  $R(N) > 1$  for some intermediate value.
- Whether this is good or bad depends on your goal

*Stochastic effects*

- The world is complicated and biological populations are not perfectly predictable
- Real populations don't go smoothly to equilibria, instead they bounce around (or sometimes do other wild stuff)
- We divide stochastic (or random) effects into demographic and environmental stochasticity

*Example*

- Female butterflies of a certain species lay 200 eggs on average, of which:
  - Half are female
  - 50% hatch successfully into larvae
  - 10% of larvae successfully pupate
  - 60% of pupae become adults
  - Half of adult females successfully reproduce
- A single gravid (pregnant) female butterfly is blown away by a freak storm, and lands by chance on a suitable island with no butterflies
- What do you expect to happen?

*Butterfly example*

- Depending on unknown conditions, especially in that first season, all of those probabilities could change dramatically
- Even if we knew the *probabilities*, that would not guarantee an exact result
- What if  $\lambda < 1$ ?

*Demographic stochasticity*

- **Demographic** stochasticity is stochasticity that operates at the level of individuals

- Individuals don't increase gradually, they die or give birth
- Individuals don't produce 1.2 offspring: they produce 0, 1, 2 or 3
- ...
- Even if we control conditions perfectly, we can't exactly predict the dynamics of small populations
- Demographic stochasticity averages out in large populations
- Important in extinction, disease trough dynamics

### *Environmental stochasticity*

- **Environmental** stochasticity is stochasticity that operates at the level of the population
- e.g., weather, pollution
- Environmental stochasticity can have large effects on any population
- But small populations are the ones in danger of going extinct

### *References*

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