

HOMEWORK #4

Due: December 1 (Friday) by 5pm

Instructions:

- The assignment consists of *two* questions, worth 4 and 6 points.
- Submit your assignment *electronically* (via Email) to the address `math2e03@math.mcmaster.ca`; hardcopy submissions will not be accepted.
- It is obligatory to use the MATLAB template file available at `http://www.math.mcmaster.ca/~bprotas/MATH2E03/template.m` (see also the link in the “Computer Programs” section on the left); submissions non compliant with this template will not be accepted.
- Make sure to enter your name and student I.D. number in the appropriate section of the template.
- Late submissions and submissions which do not comply with these guidelines will not be accepted.

1. Consider the following model of *seasonal* fishing

$$\begin{aligned}x_n^* &= x_{n-1} + R_1 x_{n-1} \left(1 - \frac{x_{n-1}}{K}\right) \\x_n &= x_n^* - q_1 U x_n^*\end{aligned}\tag{1}$$

where x_n^* and x_n are the fish population in year n before and after the fishing season. Assuming the initial value $x_0 = 0.1$ and the following values of the parameters: $K = 1.0$ (carrying capacity of the environment), $R_1 = 2.0 \cdot 10^{-3}$ (increase per year of the population), $q = 8.5 \cdot 10^{-3}$ (catchability) and $U = 10$ (size of the fishing fleet)

- (a) determine the values of $\{x_n, x_n^*\}$ during the first $N = 20$ years; plot the result as a single line using both x_n and x_n^* (use the convention that the values x_n correspond to full years, i.e., $\{0, 1, \dots, N\}$, whereas the values x_n^* correspond to “half-years”, i.e., $\{\frac{1}{2}, 1 + \frac{1}{2}, \dots, N + \frac{1}{2}\}$)
- (b) repeat this calculation assuming that U is now a function of time give by $U(t) = 10(1 + t)$; plot this solution on the same figure as in part (a).

(4 points)

2. You are given two companies with the following payscales

Employee	Qualification (years)	Compensation (\$)
A	3	32K
B	5	42K
C	10	50K
D	12	60K

Table 1: Company A

Employee	Qualification (years)	Compensation (\$)
X	2	98K
Y	4	120K
Z	9	200K

Table 2: Company B

Using log–log least square fits

- determine which of the two companies adheres more closely to the principle of formal justice (base your answer on the *average* value of the least–square error obtained in the two cases).
- for each company plot the data points together with the best fit functions (use linear coordinates and a single figure).

HINT —refer to <http://mathworld.wolfram.com/LeastSquaresFitting.html> for additional details regarding least square fits (specific formulas, etc.).

(6 points)