

**QUIZ #1**

10:30am, October 25 (Friday), 20 minutes, 10 points max  
(no books, no notes)

Write your name and Email address on the top of this sheet  
Write your answers on the reverse side and/or attach additional sheets as  
necessary.

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1. Suppose the flow domain is two-dimensional (2D) and unbounded, i.e.,  $\Omega = \mathbb{R}^2$ . Given a suitable vorticity field  $\omega = \omega(x, y)$  and knowing that the fundamental solution of the Laplace equation in 2D has the form

$$G(x, y, x', y') = -\frac{1}{2\pi} \ln \sqrt{(x - x')^2 + (y - y')^2},$$

derive the corresponding Biot-Savart law allowing one to determine the velocity field  $\mathbf{u} = [u, v]$ , such that  $\omega = \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y}$ .