

The test

- The second test is scheduled for Nov. 14 at 10:30 am (that is class time). The test will be 50 minutes.
- If your surname is in the range A - O then you will write the test in T28/001; P - Z will write in T29/101.
- The test will be multiple choice and you will need to bring an HB pencil. You will be allowed to have the McMaster approved Casio fx-991 MS but no other aids. Please bring your ID card with you to the test.
- The test will cover sections 5.1 - 5.2, 5.5, 3.1 - 3.5 and 10.1 - 10.3 from the 9th edition. I will post additional problems.
- There is a practice test for Test 2. Please try the practice test once you have studied for the test; I will post the solutions on Monday.
- There is a review class which will be run by Matt on Thursday, Nov. 13, 5:30 - 7:30 in HH 302; the class Wed. Nov. 12 will also be review.

Definition

Suppose that V is a non-empty set, $+$ is function on pairs from V and for every $k \in \mathbb{R}$ and $u \in V$, ku is defined. We say that V together with these operations defines a vector space if the following axioms are satisfied for all $u, v, w \in V$ and $k, m \in \mathbb{R}$:

Vector spaces, cont'd

- 1 $u + v \in V$.
- 2 $u + v = v + u$
- 3 $u + (v + w) = (u + v) + w$
- 4 there is a $0 \in V$ such that $u + 0 = u$ for all $u \in V$
- 5 there is a $-u \in V$ such that $u + (-u) = 0$
- 6 $ku \in V$
- 7 $k(u + v) = ku + kv$
- 8 $(k + m)u = ku + mu$
- 9 $k(mu) = (km)u$
- 10 $1u = u$

Theorem (4.1.1)

*Suppose that V is a vector space, $v \in V$ and k is a scalar.
Then*

- 1 $0v = 0$;
- 2 $k0 = 0$;
- 3 $(-1)v = -v$; and
- 4 if $kv = 0$ then either $k = 0$ or $v = 0$.

Definition

Suppose that V is a vector space and W is a non-empty subset of V . We say that W is a subspace of V if with respect to the $+$ and scalar multiplication restricted to W from V , W is a vector space in its own right.

Theorem

If V is a vector space and W is a non-empty subset of V then W is a subspace iff W is closed under $+$ and scalar multiplication.

Theorem

If V is a vector space and X is a subset of V then there is a subspace W containing X with the property that if any other subspace W' contains X then $W \subseteq W'$.

Definition

- 1 We call the W in the previous theorem the subspace spanned by X and write $\text{span}(X)$.
- 2 If $x_1, \dots, x_n \in X$ and $k_1, \dots, k_n \in \mathbb{R}$ then we call $k_1x_1 + \dots + k_nx_n$ a linear combination of elements of X .

Fact

If X is a subset of a vector space V then the set of all linear combinations of elements of X is the subspace spanned by X .