

# LIMITS

## 1LS3 - Fall 2016/17

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Properties of limits:

1. The limit of the sum is the sum of the limits, or

$$\lim_{x \rightarrow a} [f(x) + g(x)] = \lim_{x \rightarrow a} f(x) + \lim_{x \rightarrow a} g(x) \quad (1)$$

2. The limit of the difference is the difference of the limits, or

$$\lim_{x \rightarrow a} [f(x) - g(x)] = \lim_{x \rightarrow a} f(x) - \lim_{x \rightarrow a} g(x) \quad (2)$$

3. The limit of the product of a constant,  $c$ , and a function is the product of the constant and the limit of the function, or

$$\lim_{x \rightarrow a} [cf(x)] = c \cdot \lim_{x \rightarrow a} f(x) \quad (3)$$

4. The limit of the product is the product of the limits, or

$$\lim_{x \rightarrow a} [f(x)g(x)] = \left[ \lim_{x \rightarrow a} f(x) \right] \cdot \left[ \lim_{x \rightarrow a} g(x) \right] \quad (4)$$

5. Suppose  $\lim_{x \rightarrow a} g(x) \neq 0$ . Then the limit of the quotient is the quotient of the limits, or

$$\lim_{x \rightarrow a} \left[ \frac{f(x)}{g(x)} \right] = \frac{\left[ \lim_{x \rightarrow a} f(x) \right]}{\left[ \lim_{x \rightarrow a} g(x) \right]} \quad (5)$$