

### 1. RICHARDSONS MODEL

(Mooney and Swift project 5.2, part 2, page 311)

The state variables  $x$  and  $y$  are the annual rates of expenditure, and we suppose the rates of expenditure depend positively on the expenditure of the other country (with coefficients  $a, b$ ) and negatively on ones own expenditure (with coefficients  $m, n$ , so that your expenditure would decay exponentially if the other country stopped spending). If we further assume there are underlying grievances  $r$  and  $s$  that drive an increase in expenditure even in the absence of spending by the other country: then we get

$$\frac{dx}{dt} = ay - mx + r \quad \frac{dy}{dt} = bx - ny + s$$

This project will look at part 2 a), b), c), d) from the book.