

MATH3MB3 Exam Review

For every question below:

- a) Classify the model.
- b) Find the fixed point(s) of the model.
- c) Determine the stability of the fixed point(s).

1.

$$\begin{aligned}S(t+1) &= S(t) + m[N - S(t)] - S(t)[1 - e^{-\beta I(t)}] \\I(t+1) &= I(t) + S(t)[1 - e^{-\beta I(t)}] - [m + \gamma]I(t)\end{aligned}$$

2. $N(t+1) - N(t) = R_{\max}N \frac{1-N(t)}{N_{\max}}$

3. $N(t+2) = N(t+1) + 3N(t)$

- d) Determine the time dependent solution if $N(0) = 0$ and $N(1) = 1$.

4.

$$\begin{aligned}\frac{dS(t)}{dt} &= -\mathcal{R}_0SI \\ \frac{dI(t)}{dt} &= \mathcal{R}_0SI - I\end{aligned}$$

5.

$$\begin{aligned}P(t+1) &= \gamma\alpha\sigma P(t) + \sigma\beta S(t) \\ S(t+1) &= \gamma\sigma(1-\alpha)P(t)\end{aligned}$$

6. $\frac{dx}{dt} = a - bx$

- d) Find the general solution to the model.

7. $\frac{dx}{dt} = rN(1 - \frac{N}{K})$

- d) Find the general solution to the model.

8.

$$\begin{aligned}\frac{dx_1}{dt} &= x_1 + 2x_2 \\ \frac{dx_2}{dt} &= 3x_1 + 2x_2\end{aligned}$$