

MATH 3375 (Theory of Cryptology) – Fall 2013

Homework Assignment 1

Due: September 19

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1. From Section 1.1, do Exercises 1, 3, 7.
2. From Section 1.2, do Exercises 7, 9.
3. Prove Theorem 1.1 (g) and (h).
4. Find  $\gcd(2013, 642)$ , and write the greatest common divisor as a linear combination of 2013 and 642.
5.
  - (i) Use the Euclidean algorithm to find  $\gcd(55, 34)$  and  $\gcd(144, 89)$ .
  - (ii) Describe the pattern among the remainders when you apply the division algorithm.
  - (iii) Make a conjecture about the pattern you found in part (ii). (you don't need to prove it). Find an example that verifies your conjecture.
6. Let  $a$  and  $b$  be positive integers. Prove that  $\gcd(a, b) = 1$  if and only if there exists integers  $s$  and  $t$  such that  $as + bt = 1$ .